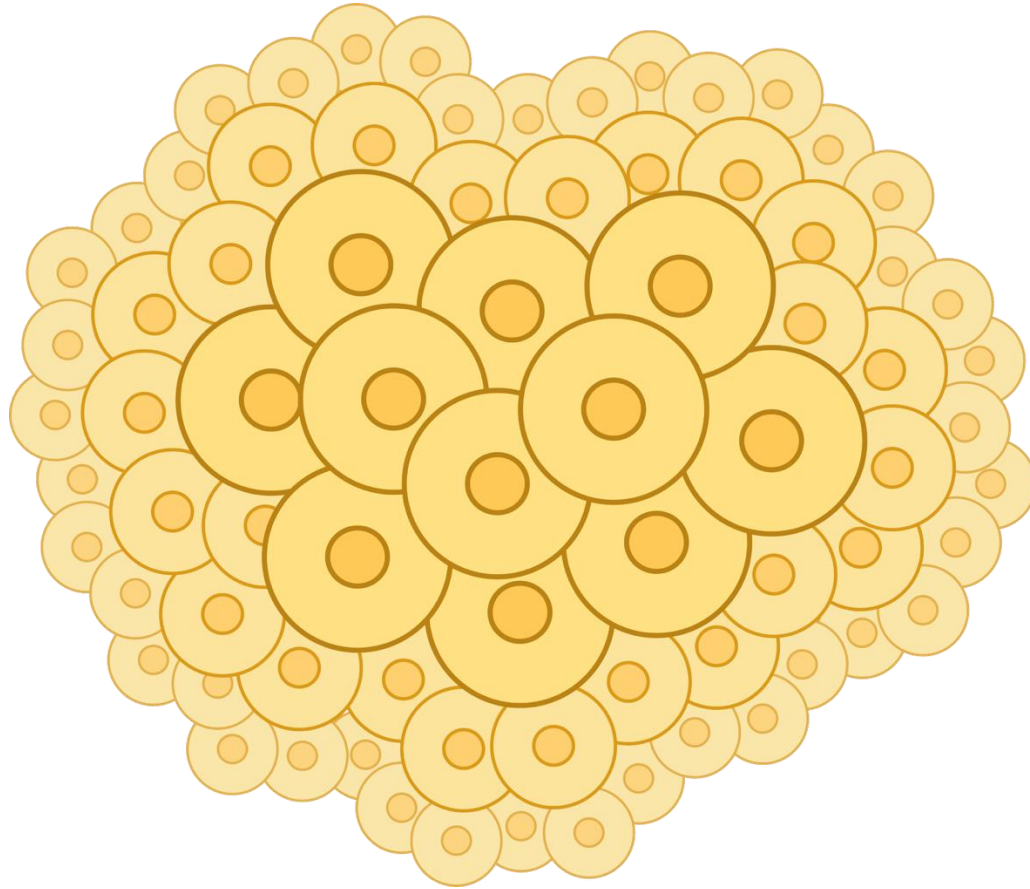


A decorative border composed of numerous overlapping circles in various colors (green, purple, yellow, pink, orange) arranged in a roughly circular pattern around the central text.

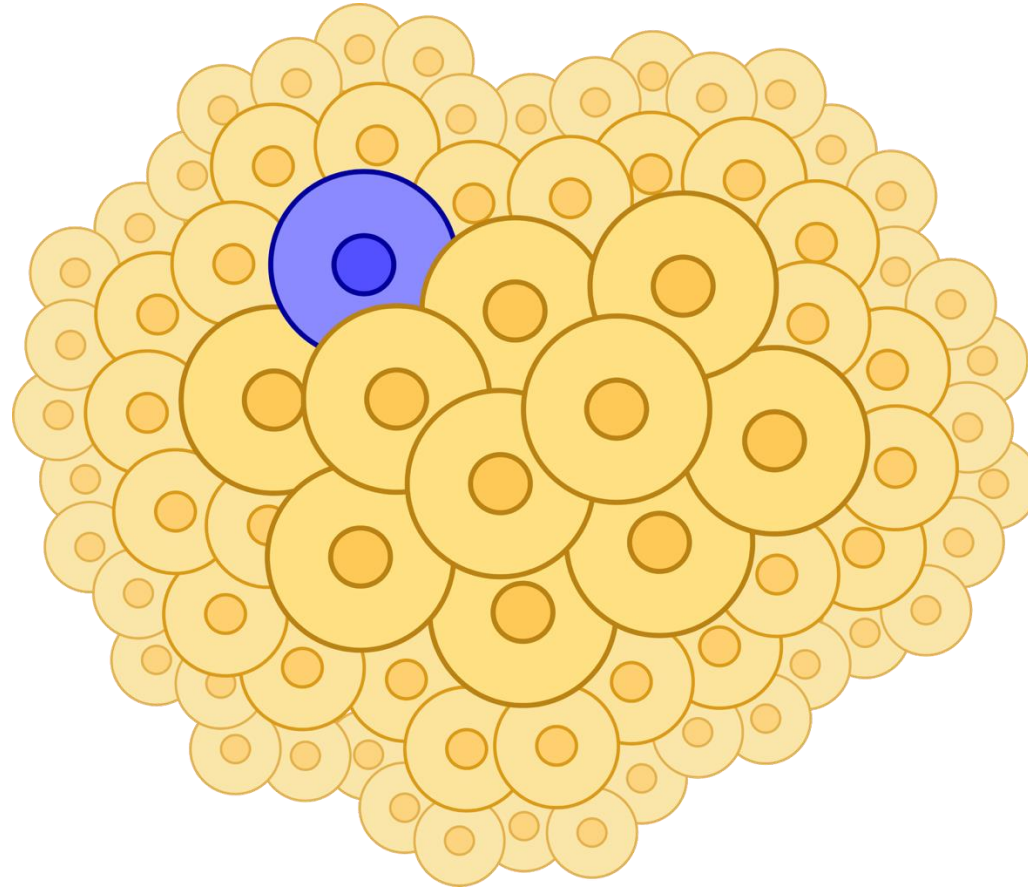
Modeling Drift and Selection in Spermatogonial Stem Cell Dynamics

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University of Utah

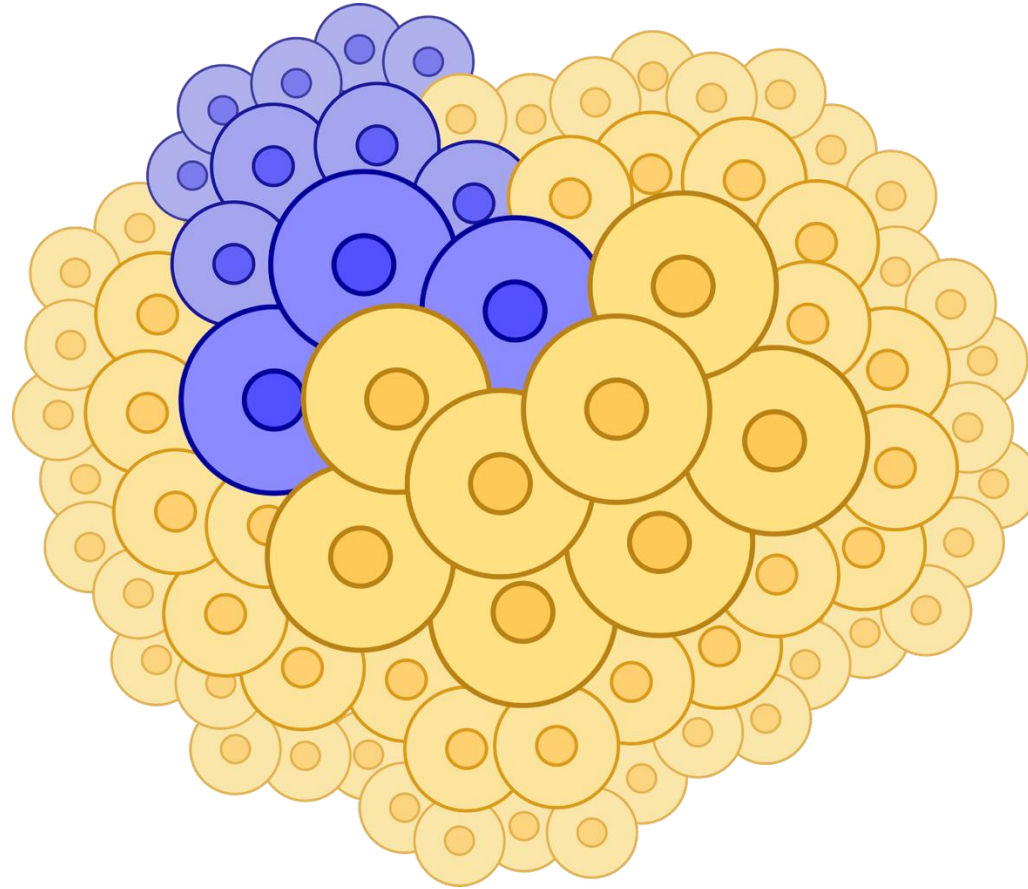
Cells in our body are constantly dividing and dying.



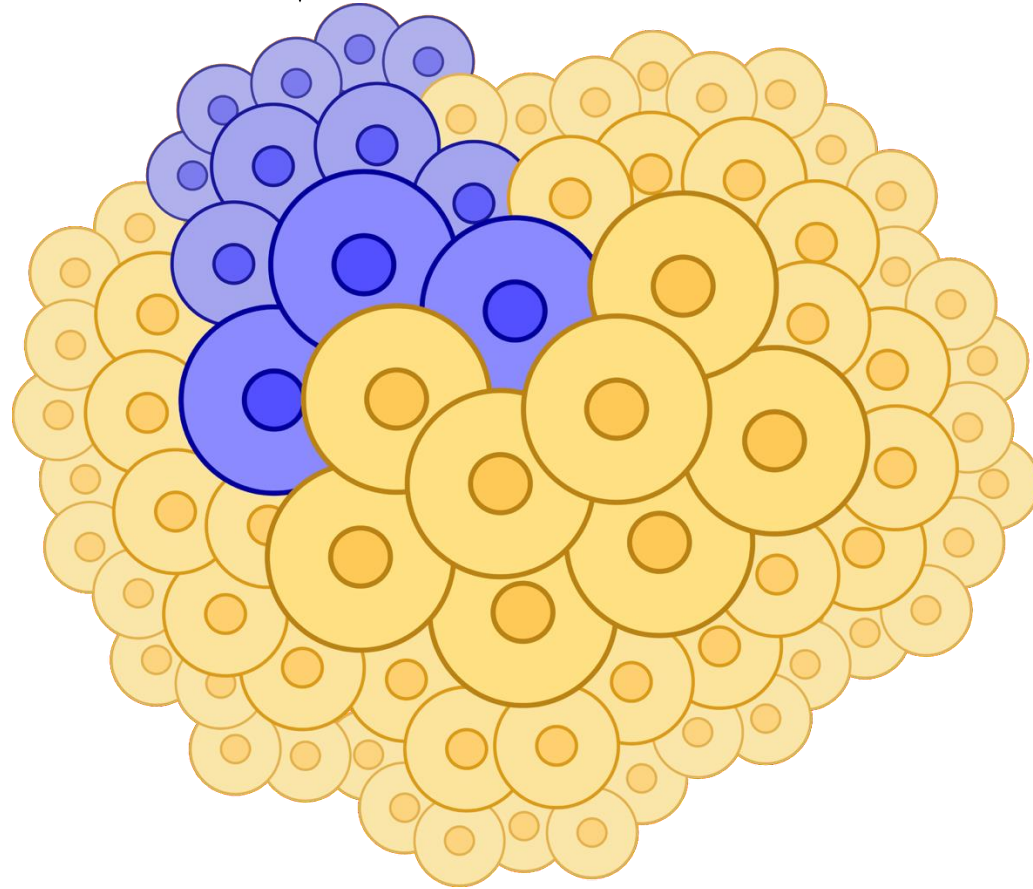
Over time, dividing cells can accumulate mutations.



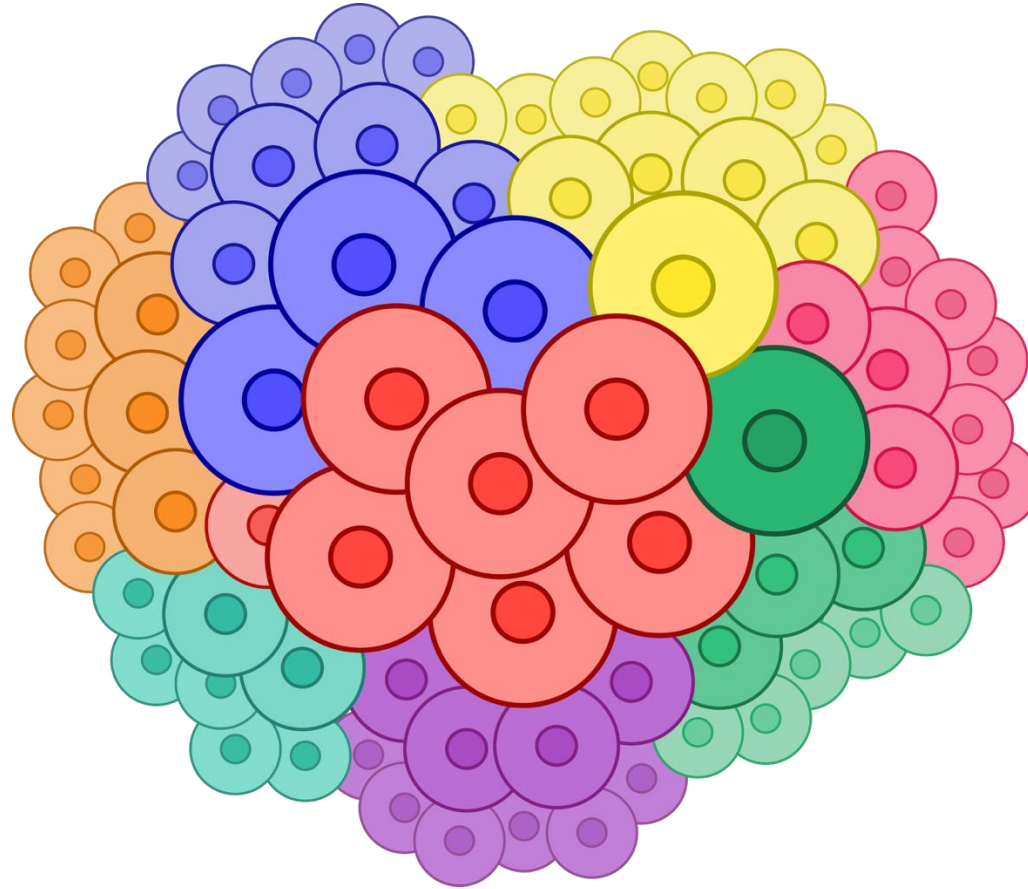
These mutations are inherited by daughter cells.



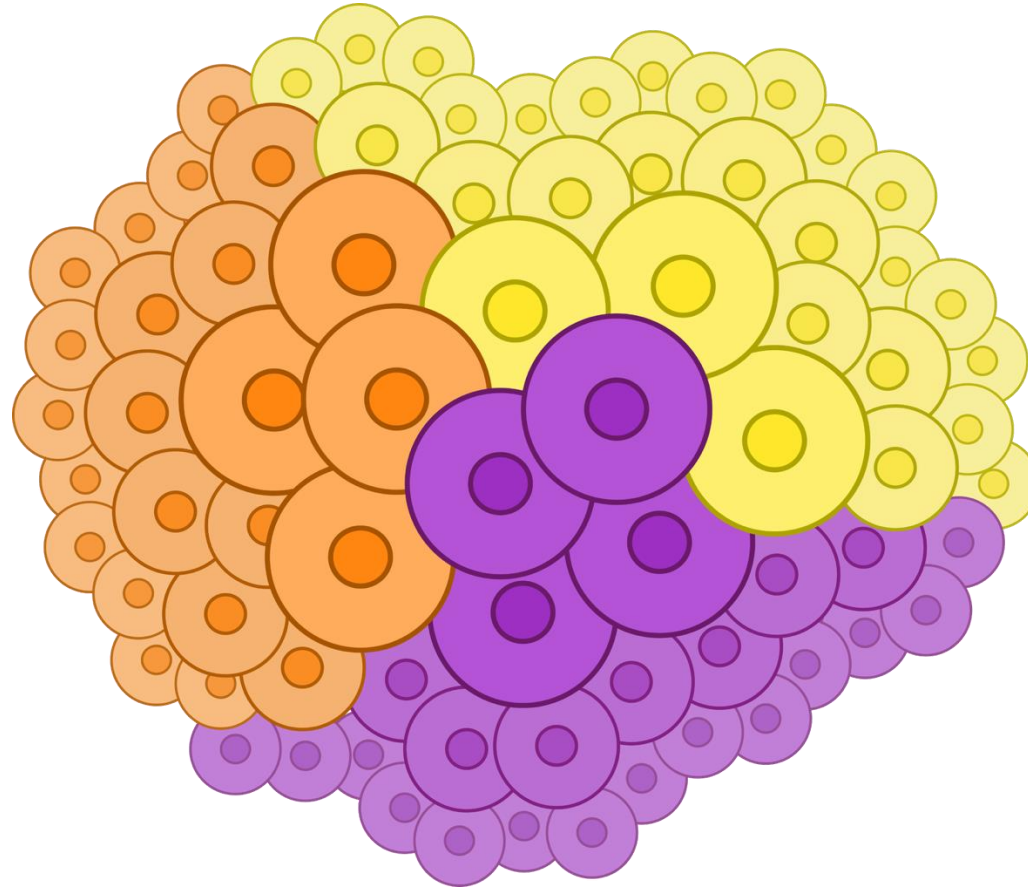
“Clone”



Our tissues are full of these clones.

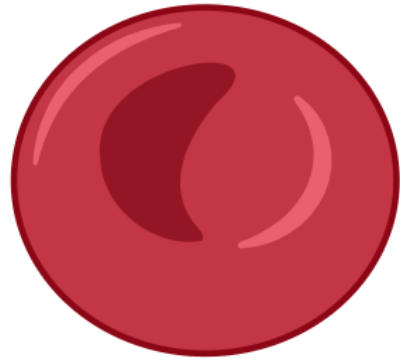


As we age, some clones begin to dominate others.



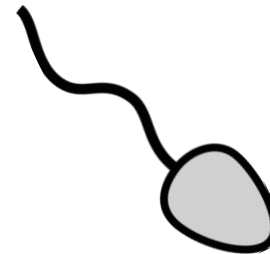
Stem cells are responsible for developing and maintaining specialized tissue.

Hematopoietic
stem cells



Red Blood Cell

Spermatogonial
stem cells

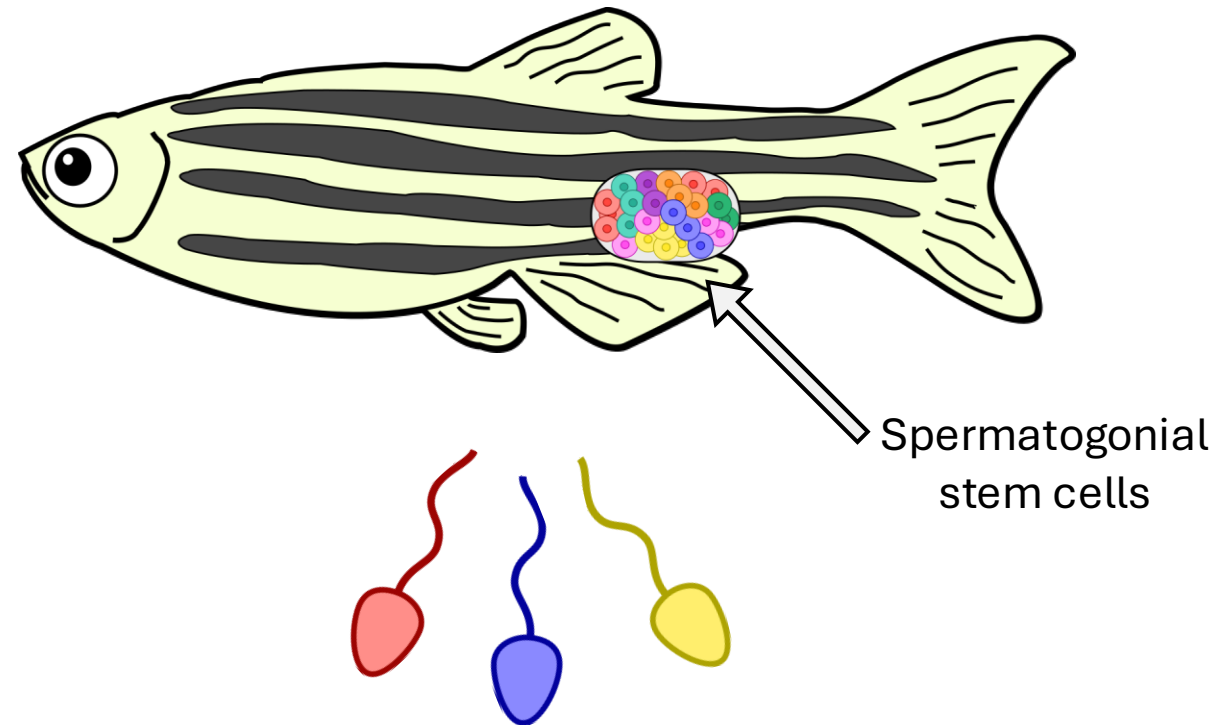


Sperm Cell

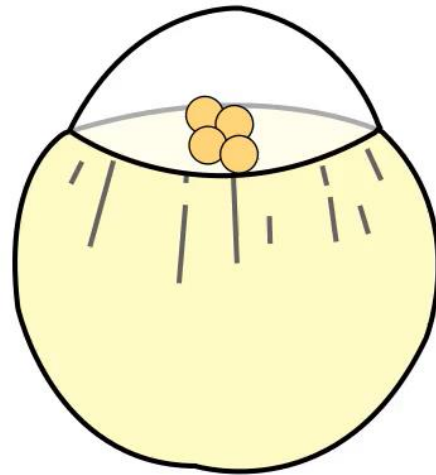
Stem cells populations are hard to directly study.

We use the **zebrafish testis** as a model system.

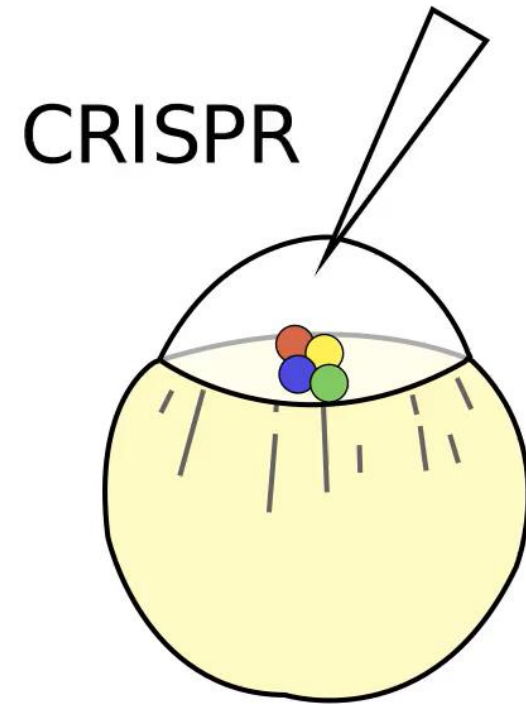
I combine models and experimental data to study clonal dynamics.



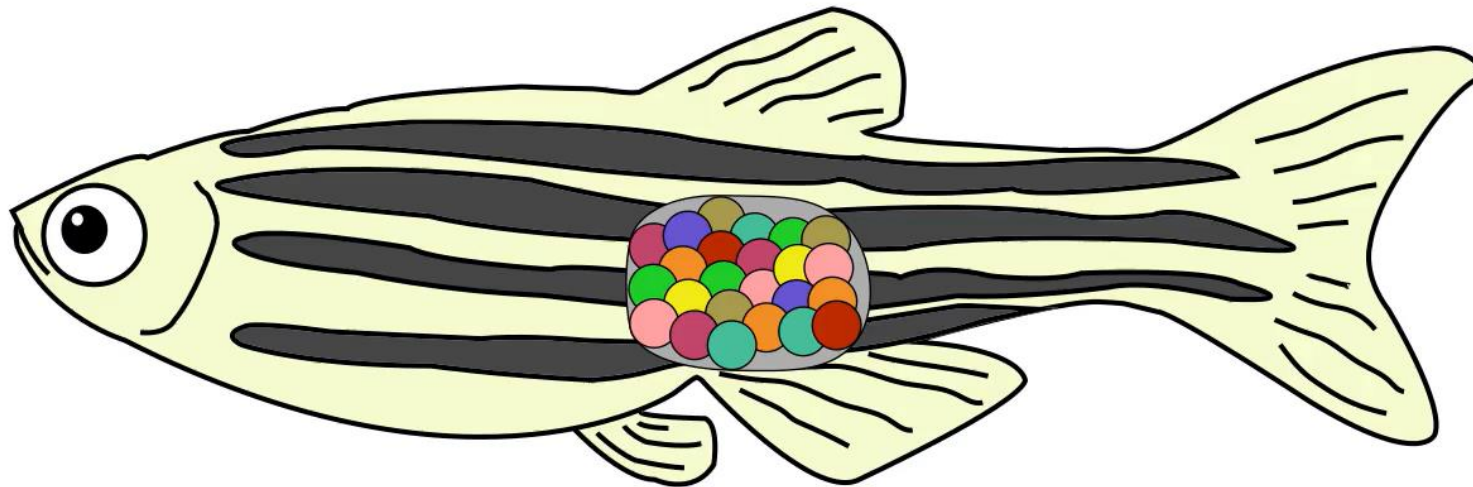
0-4 hpf

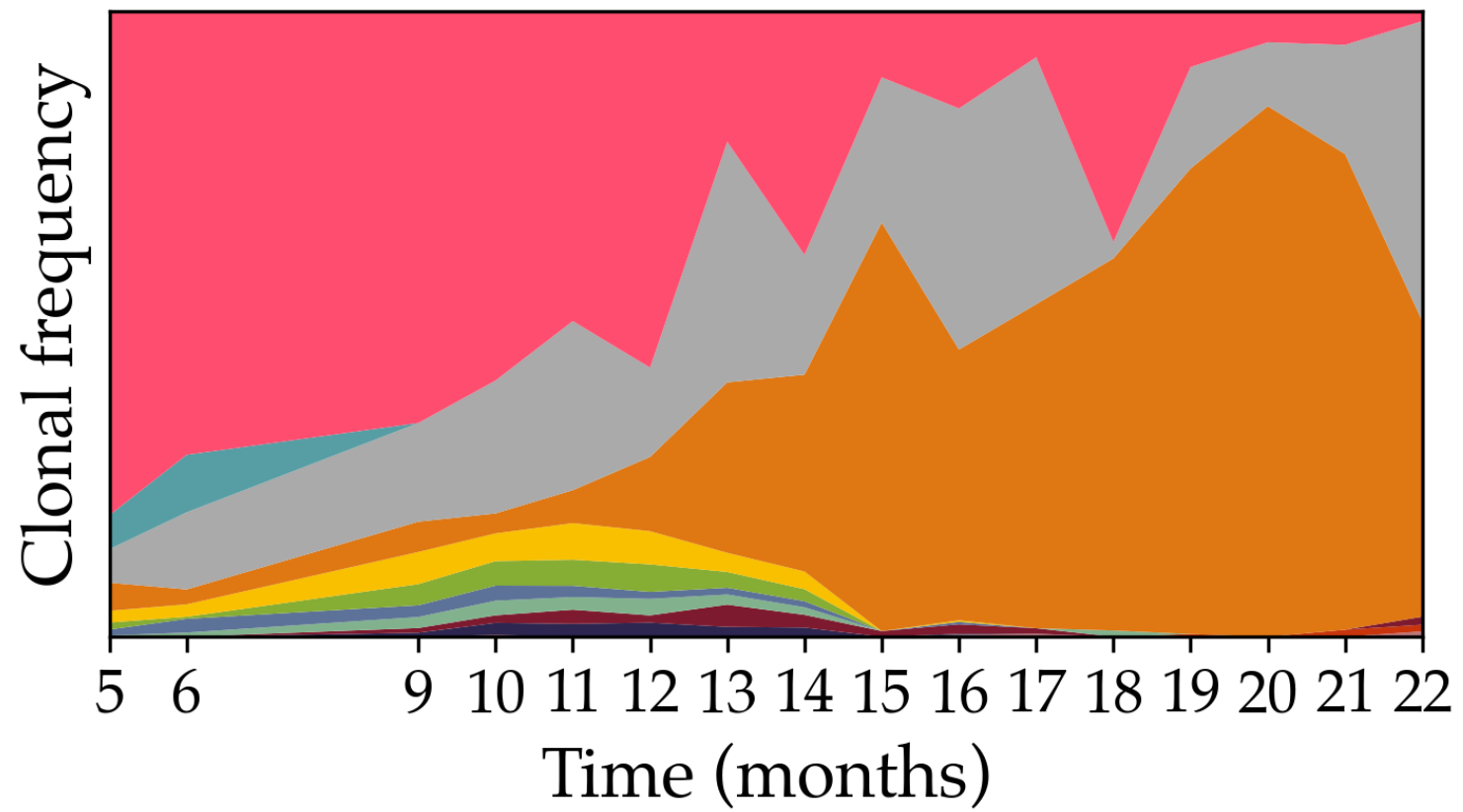


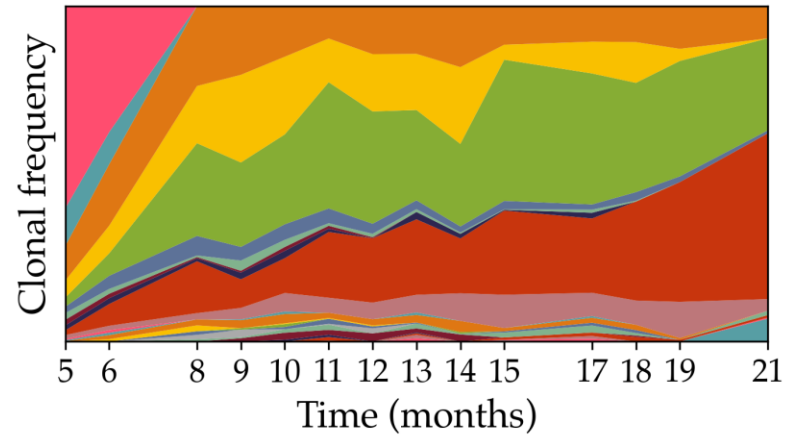
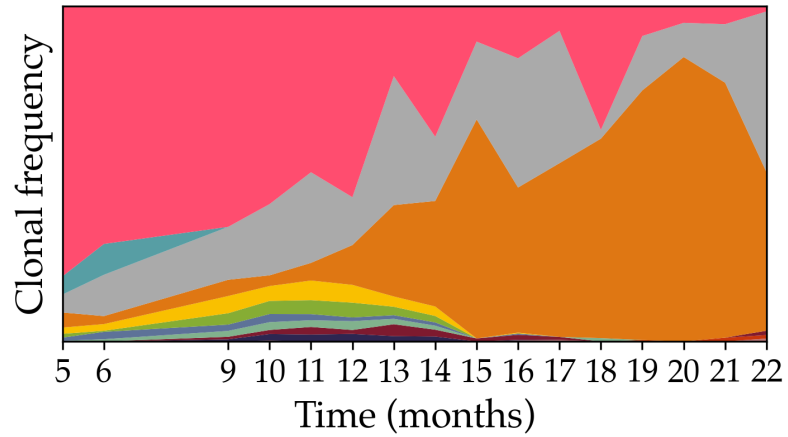
0-4 hpf



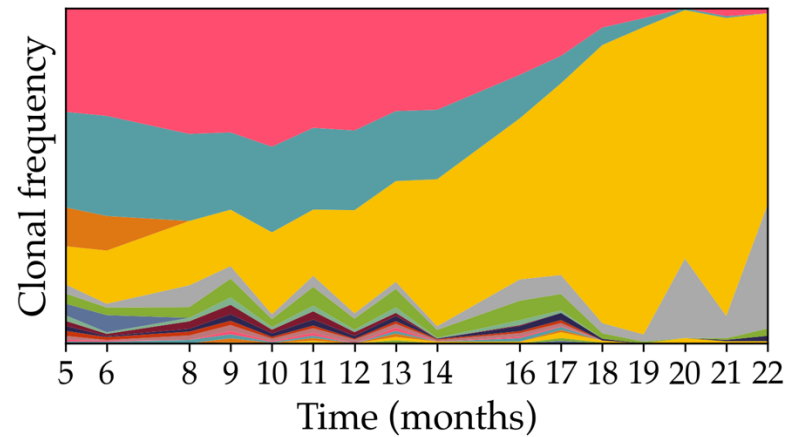
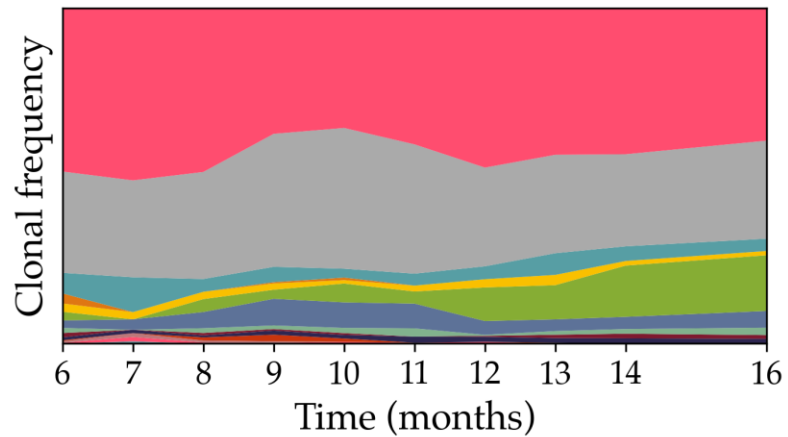
adulthood





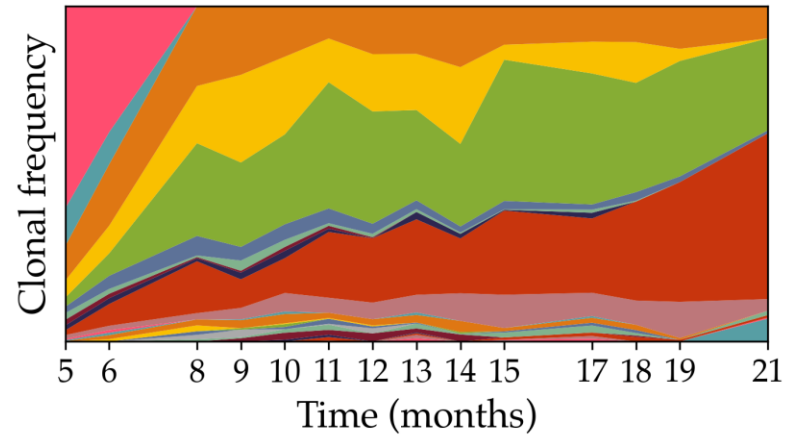
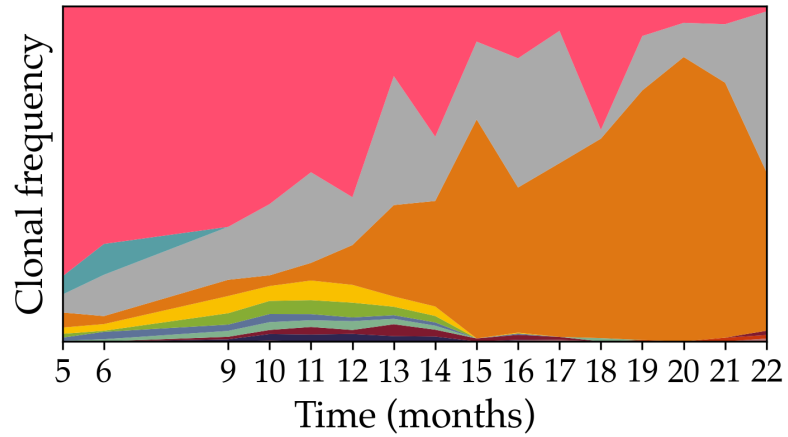


A few clones dominate the sperm pool.

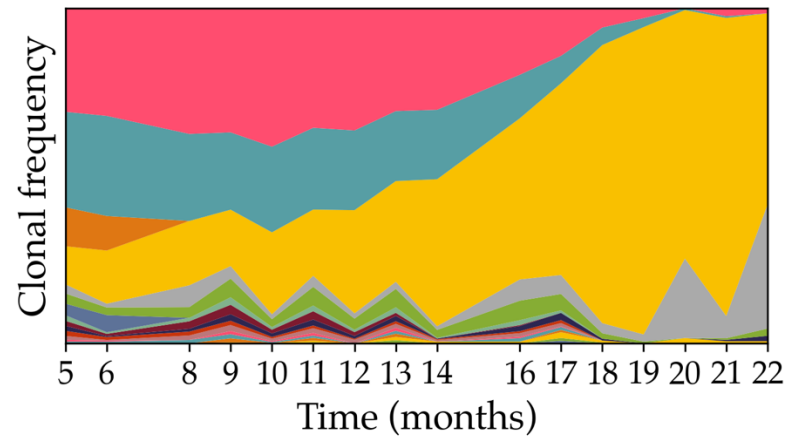
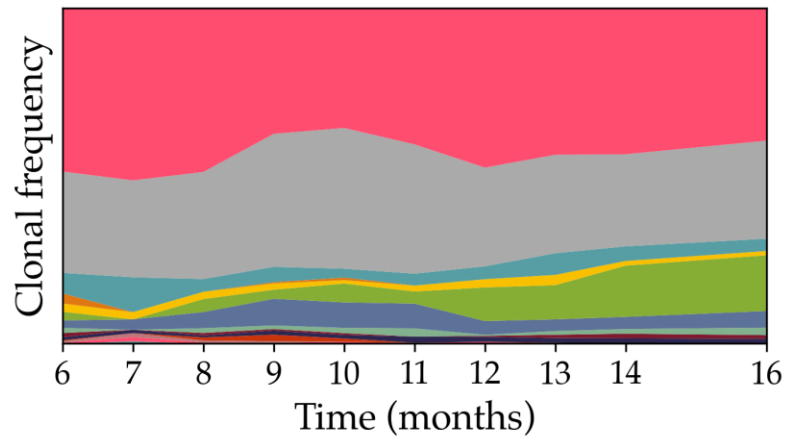


Small clones persist.

Consistent trends emerge.

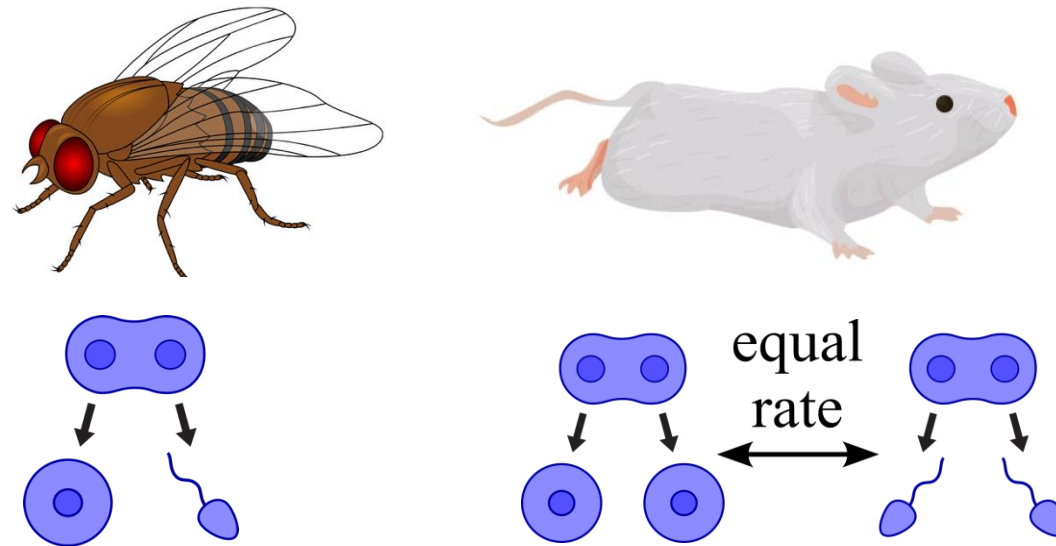


How strong is genetic **drift**?

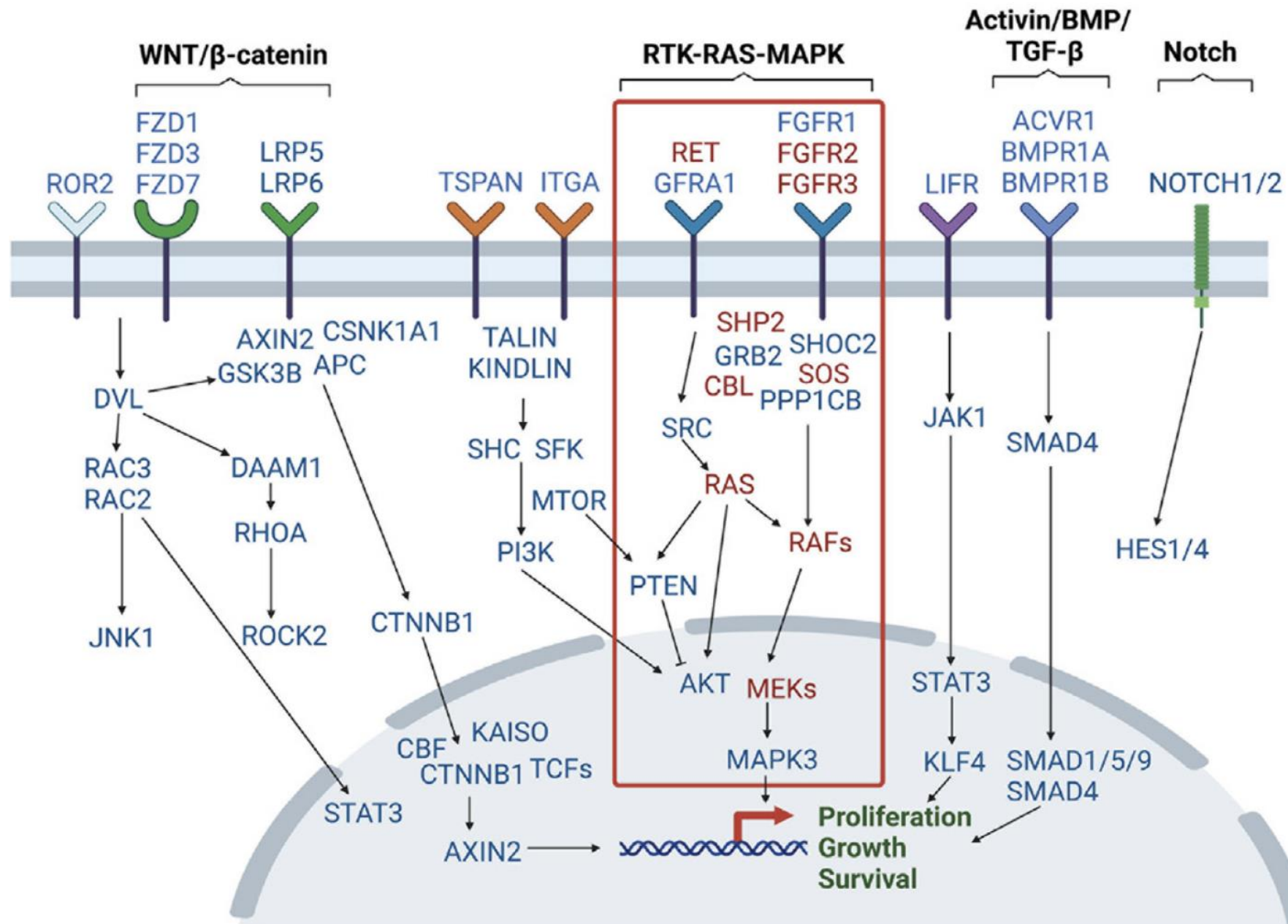


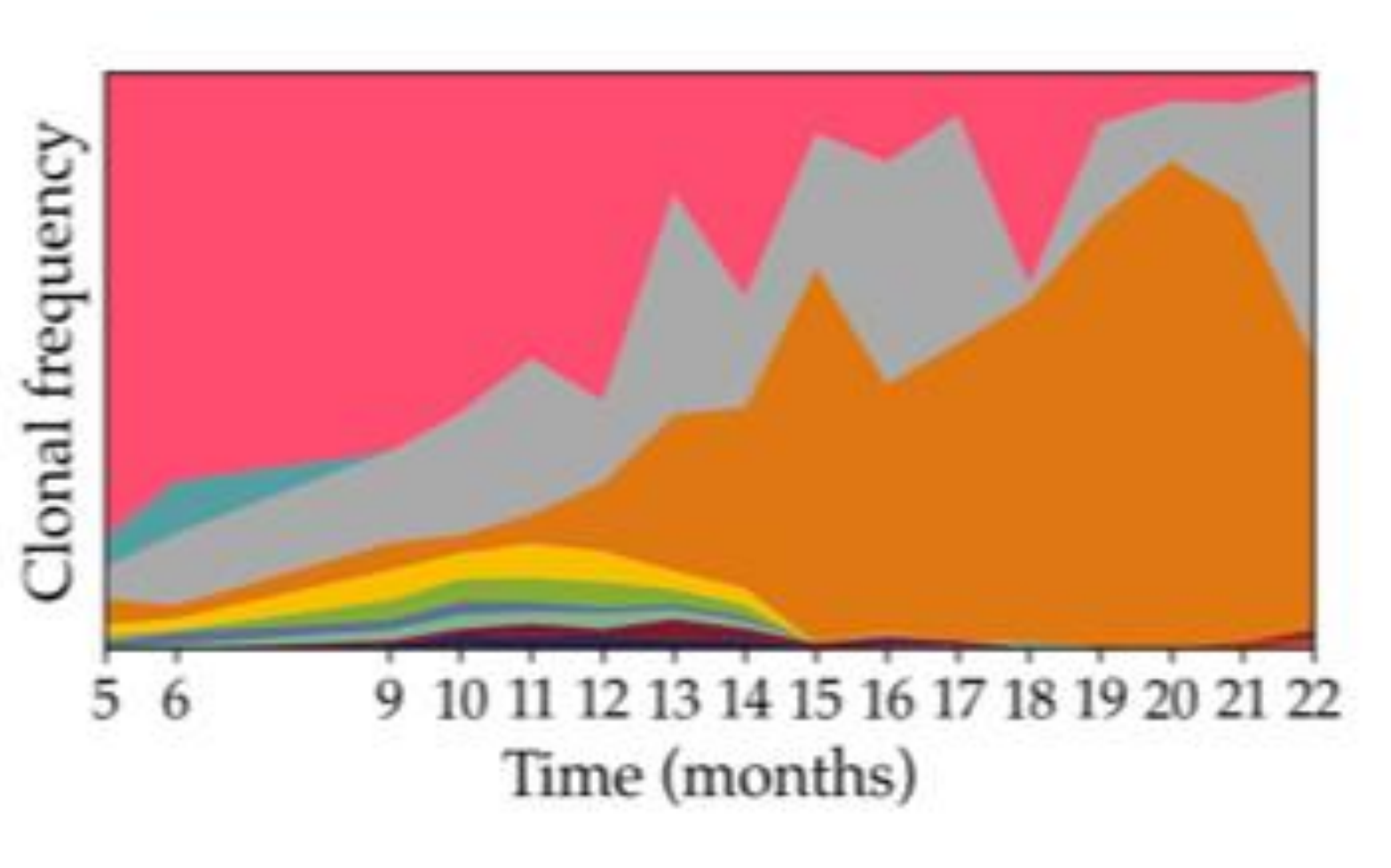
Is there evidence of **selection**?

Clonal drift is *sometimes* seen in some other organisms.

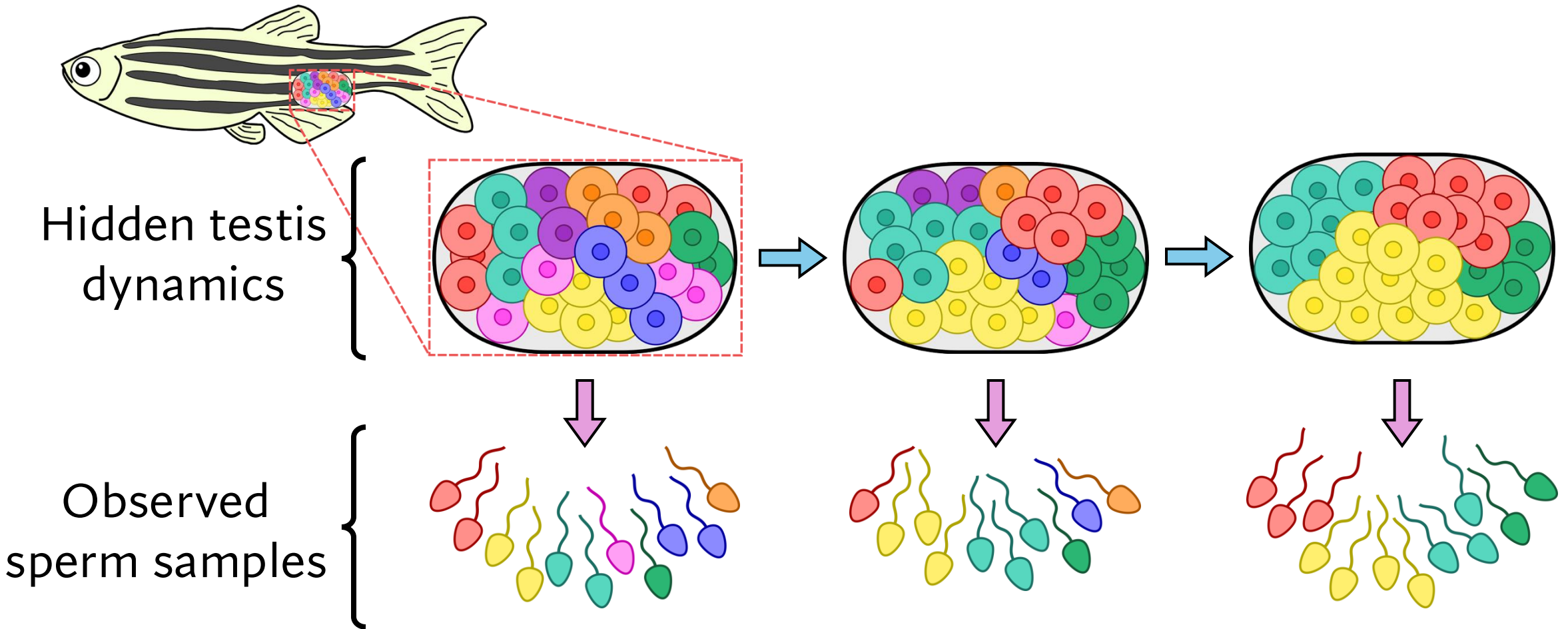


Positive selection is seen in humans through **paternal age effect** mutations.



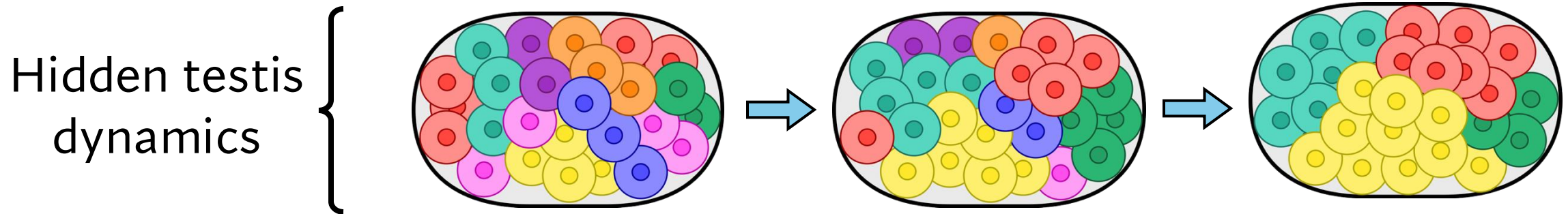


Hidden Markov modeling setup

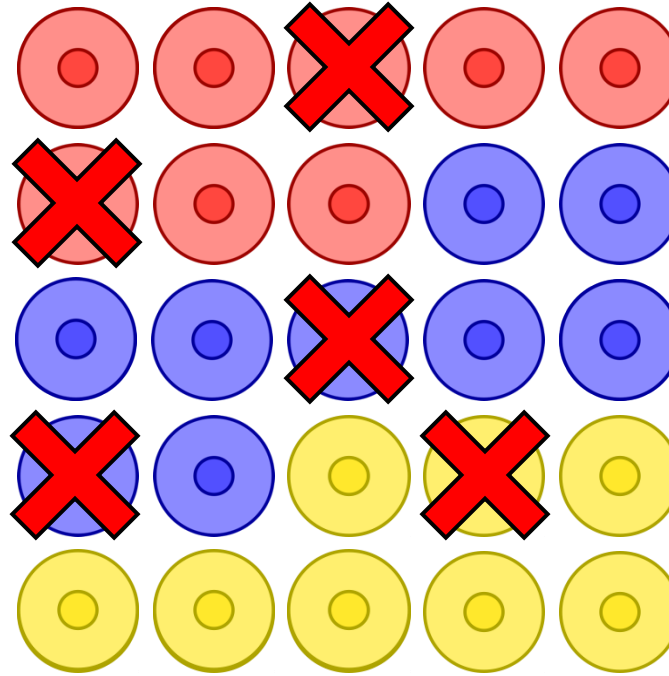


Hidden Markov modeling setup

Use the **Moran process** for the hidden dynamics.

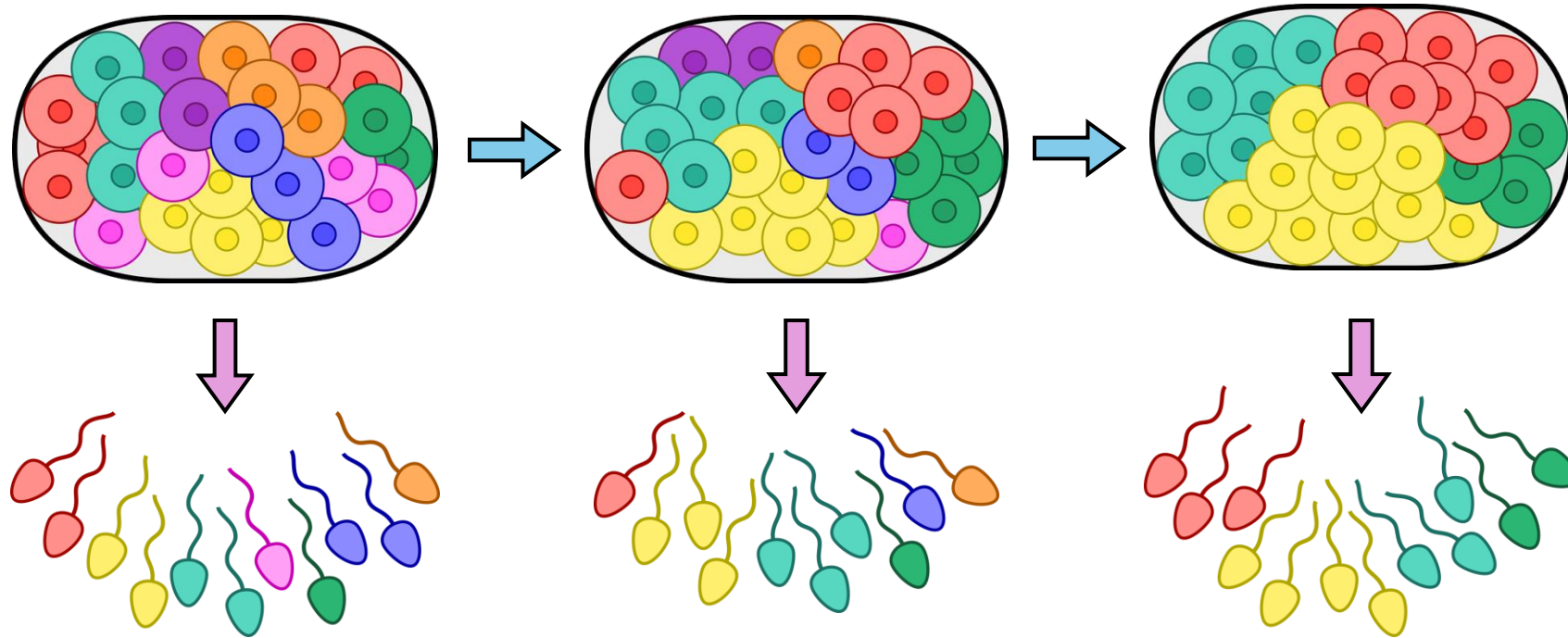


Moran process



Stem cells differentiate at rate r .
Measures strength of **genetic drift**.

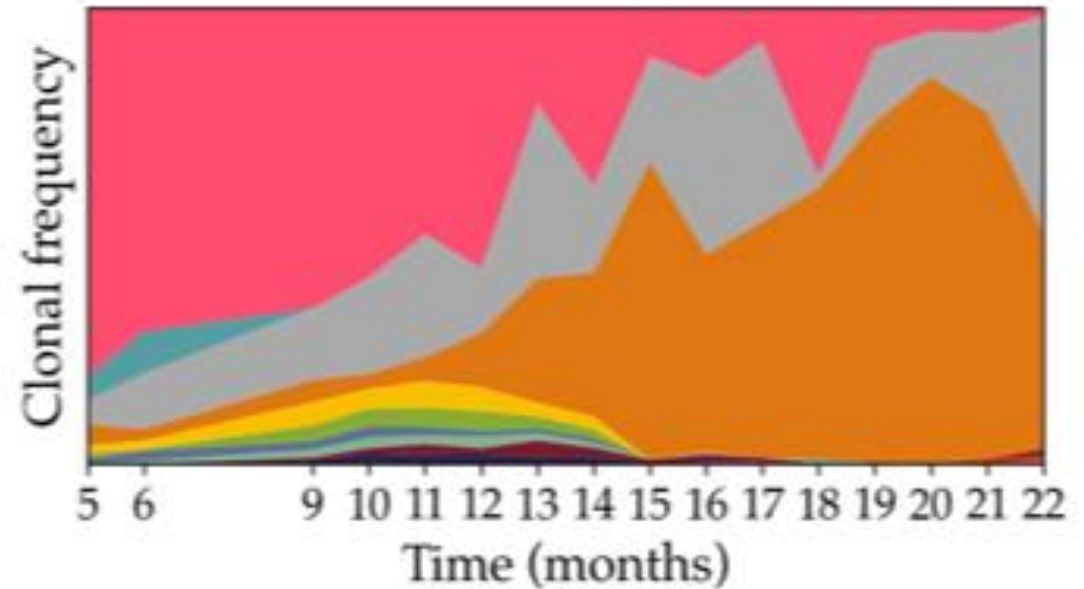
Observed sperm data



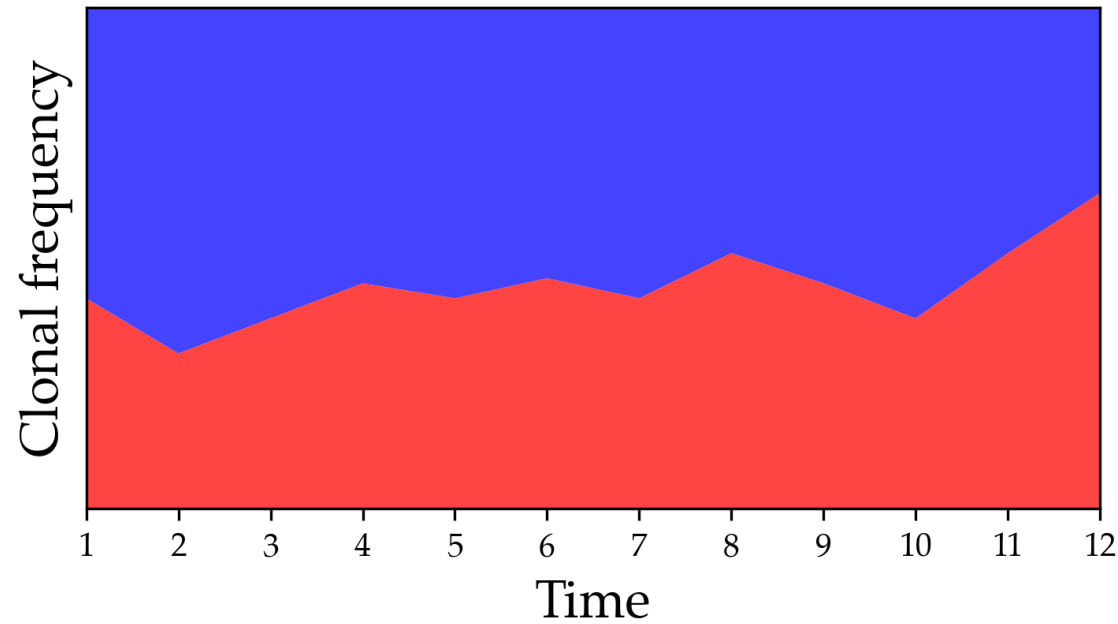
Sample stem cells with replacement!

Are clones undergoing drift?

Is the differentiation rate r non-zero?



A simple example

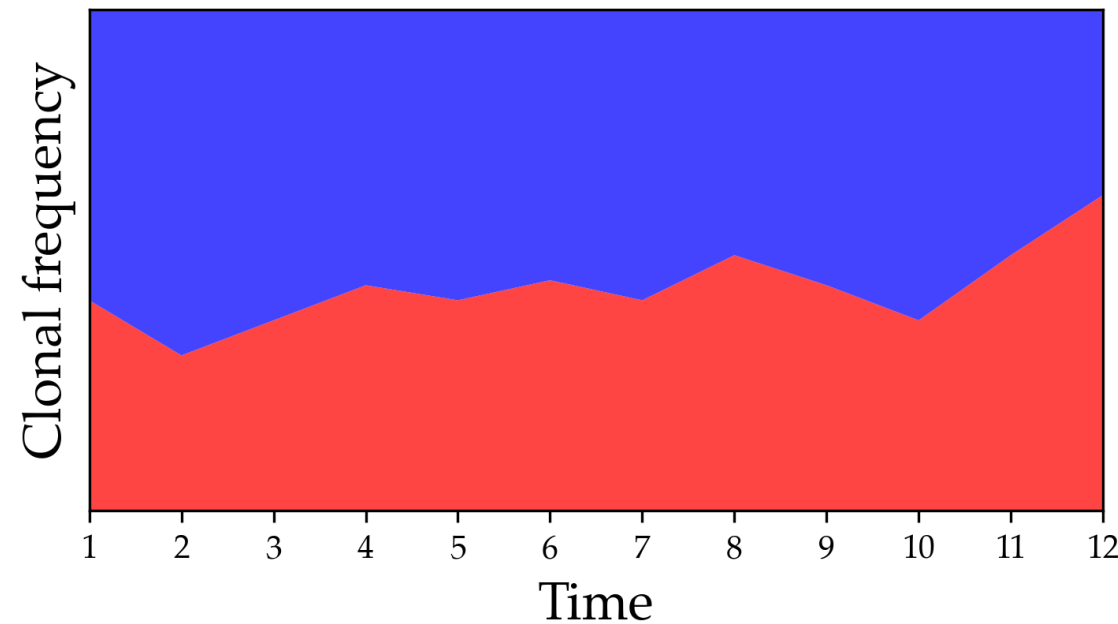


200 stem cells
100 sperm per sample

??? differentiation rate

Estimate parameters using ML (maximum likelihood)

$$\mathcal{L}(r) = \ln(\text{Pr}(\text{observed data} : \text{differentiation rate } r)).$$



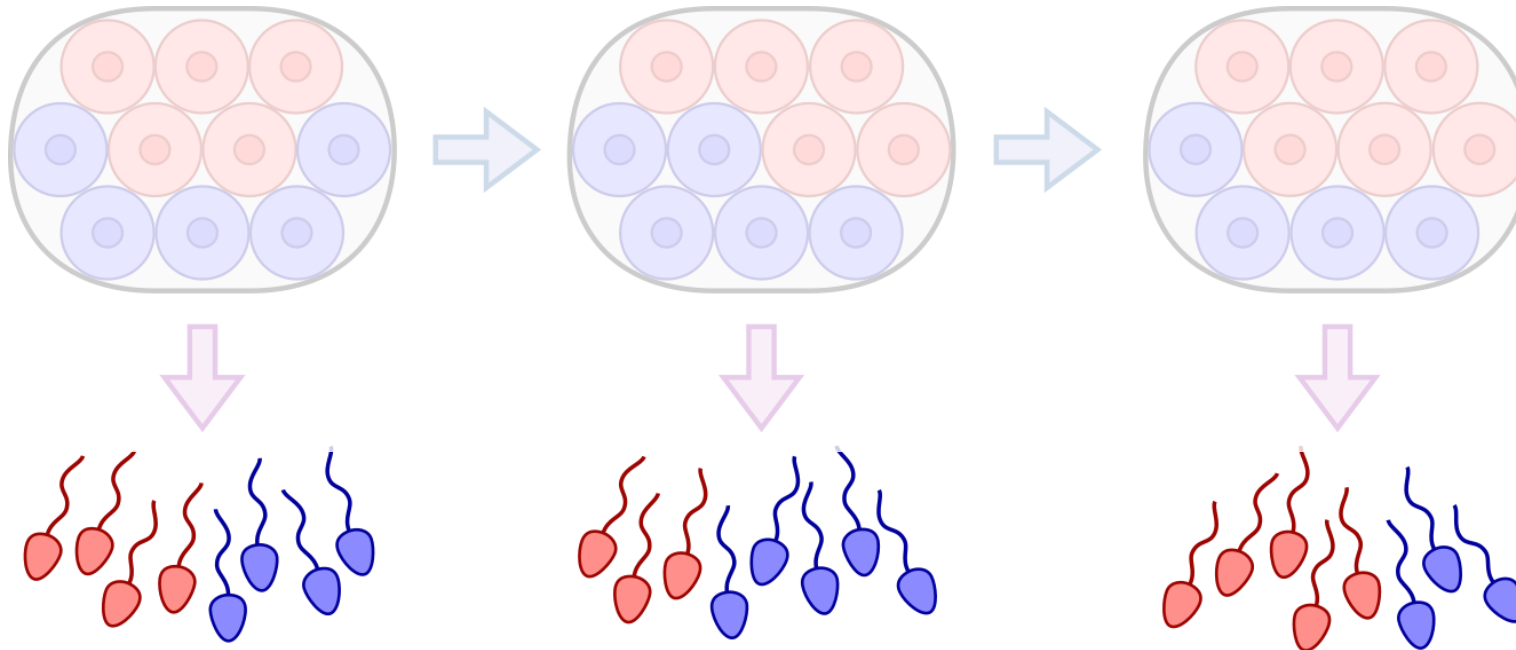
Null hypothesis: $r = 0$.

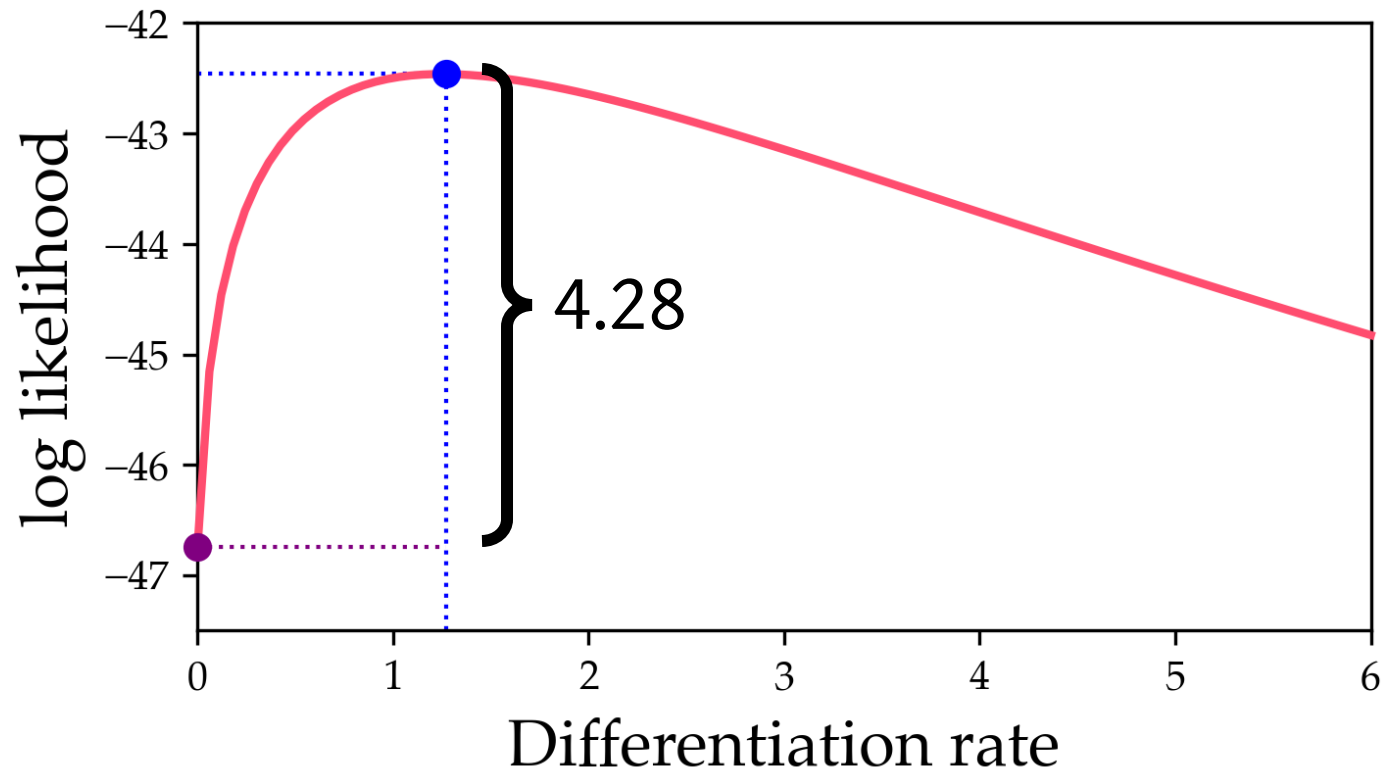
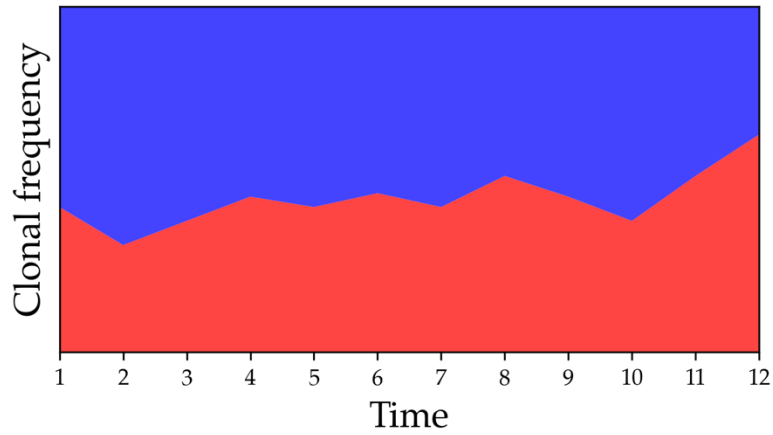
Use the log likelihood ratio
test statistic,

$$\lambda = 2(\max(\mathcal{L}) - \mathcal{L}(0))$$

We'll accept that $r \neq 0$ if $\lambda > 6$.

Likelihood calculations are made
using the **forward algorithm**.

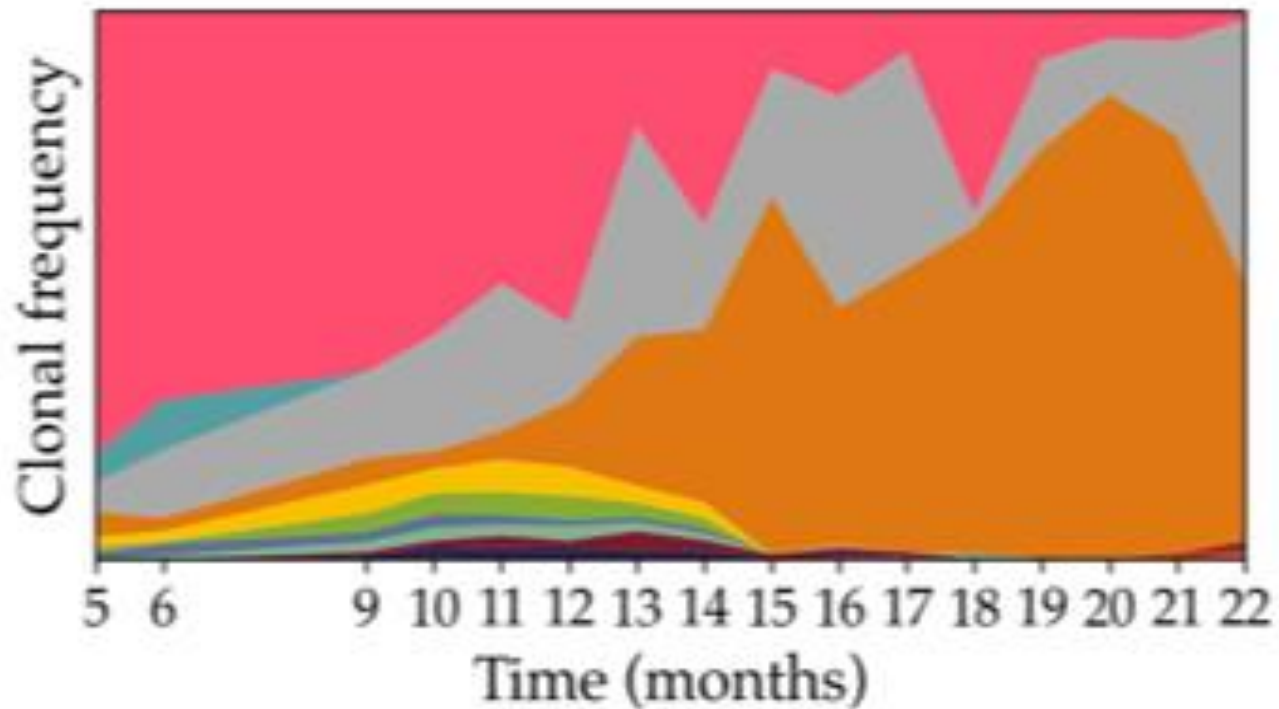




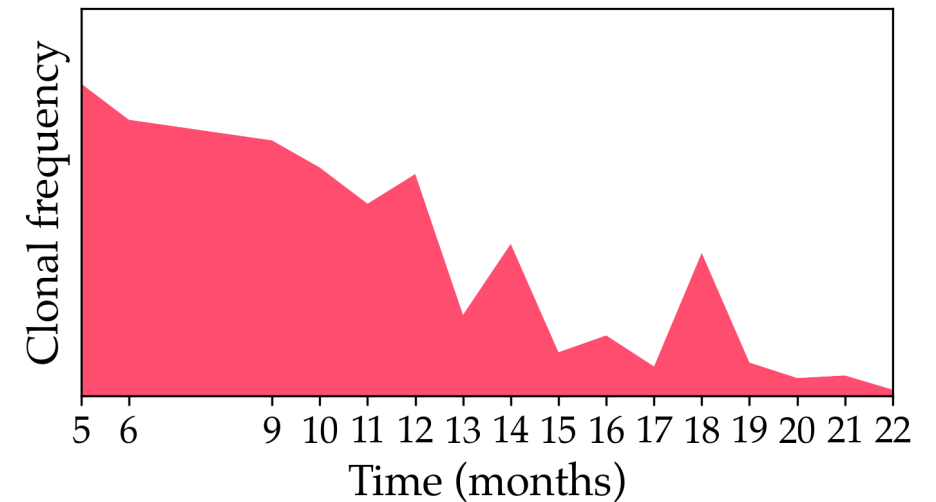
The likelihood is maximized at $r = 1.25$.

The test statistic λ is 8.57.

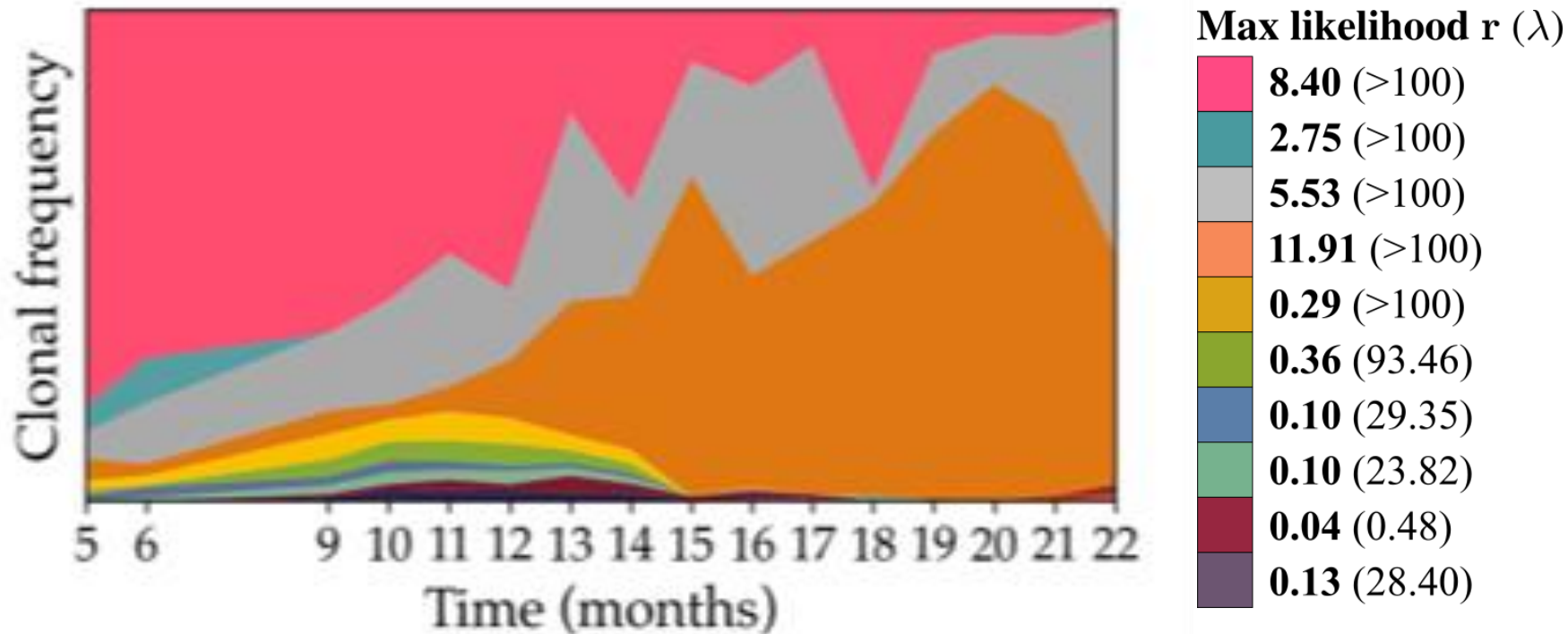
Measuring genetic drift in experimental data

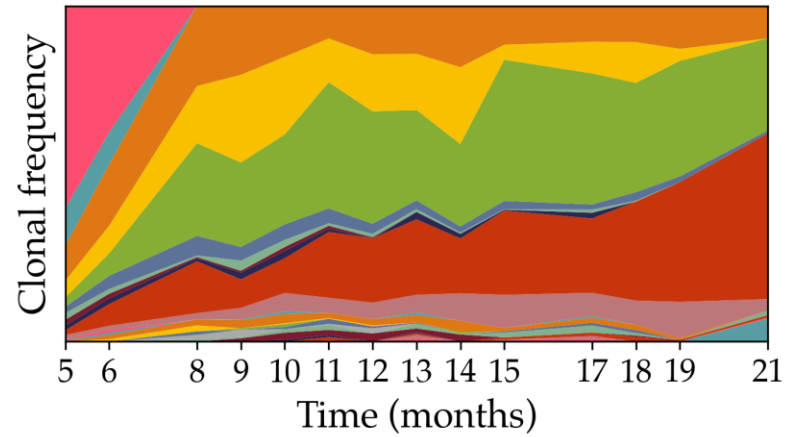
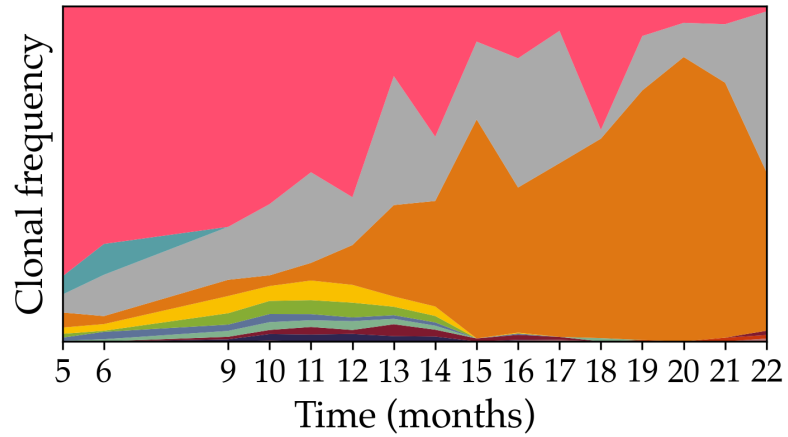


Estimate drift of each clone individually.

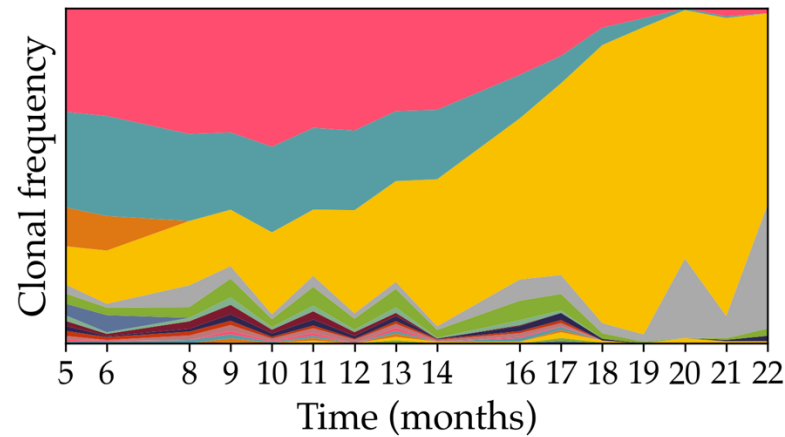
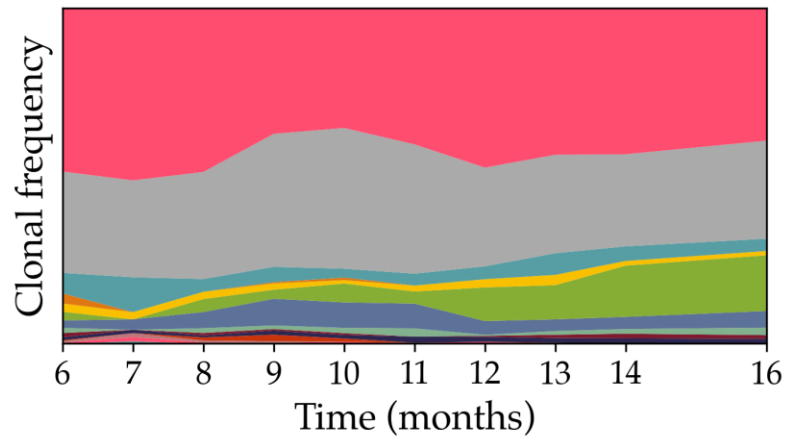


Measuring genetic drift in experimental data



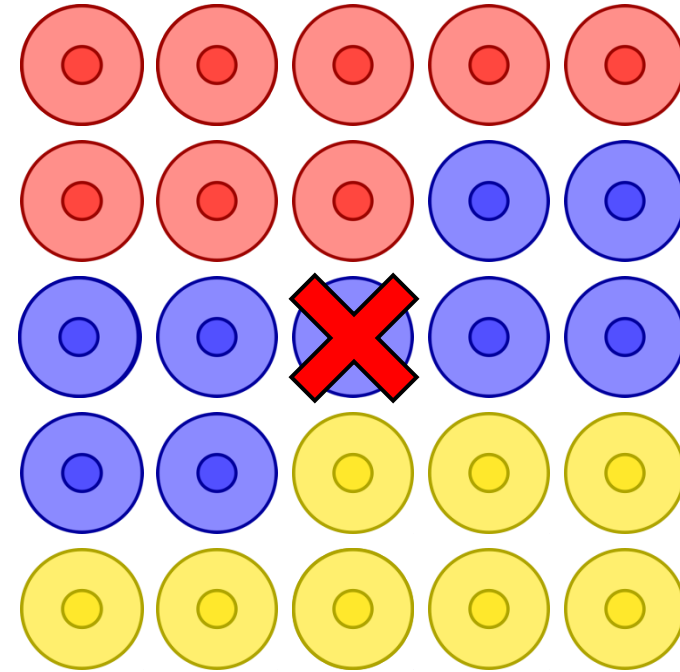
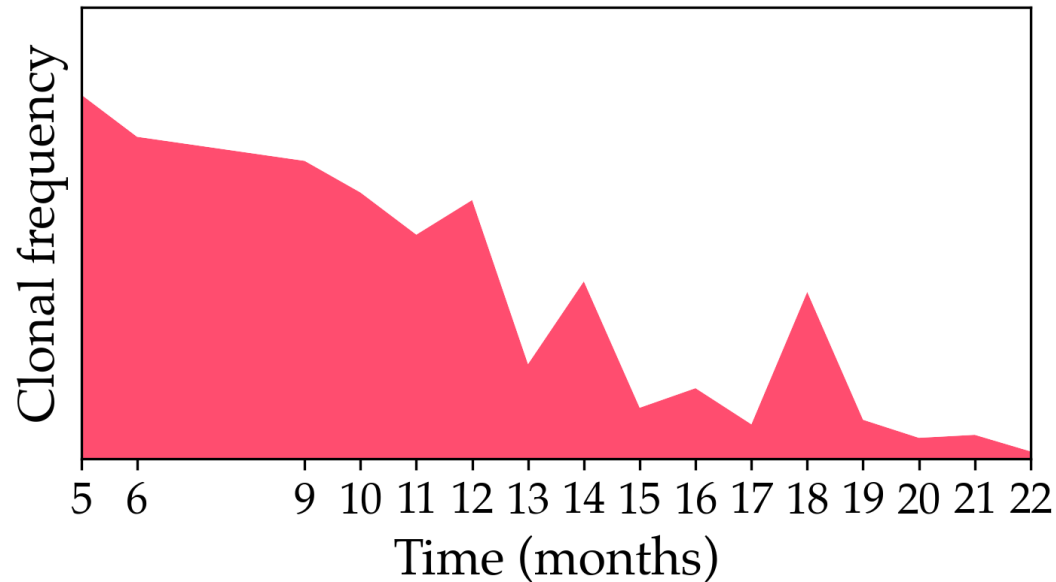


Large clones
experience more drift
than small clones.

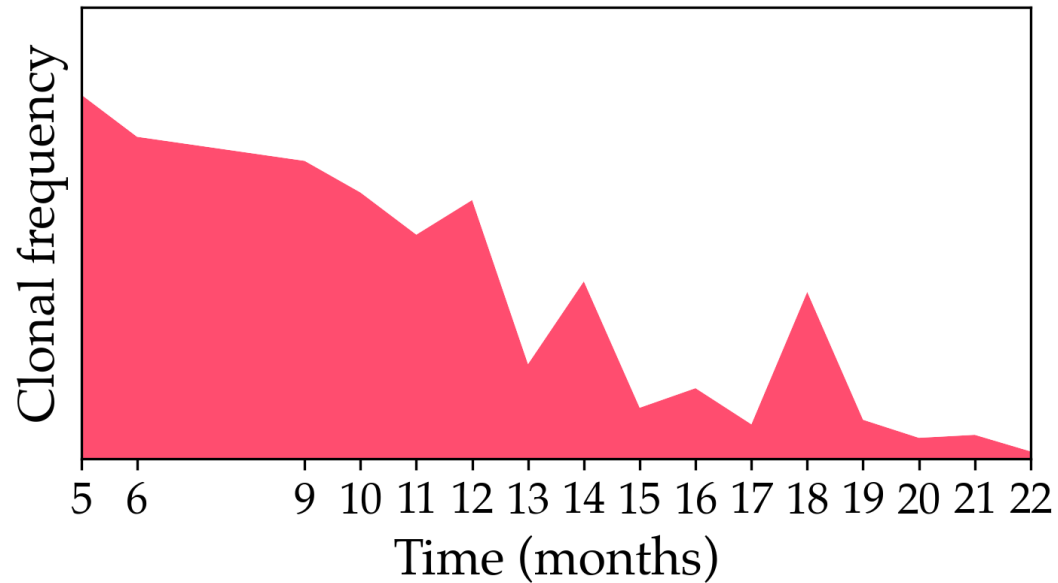


Clones that begin
large tend to
decrease in size.

Is there evidence of selection?



Weigh probability of a target clone dividing by $1 + s$.



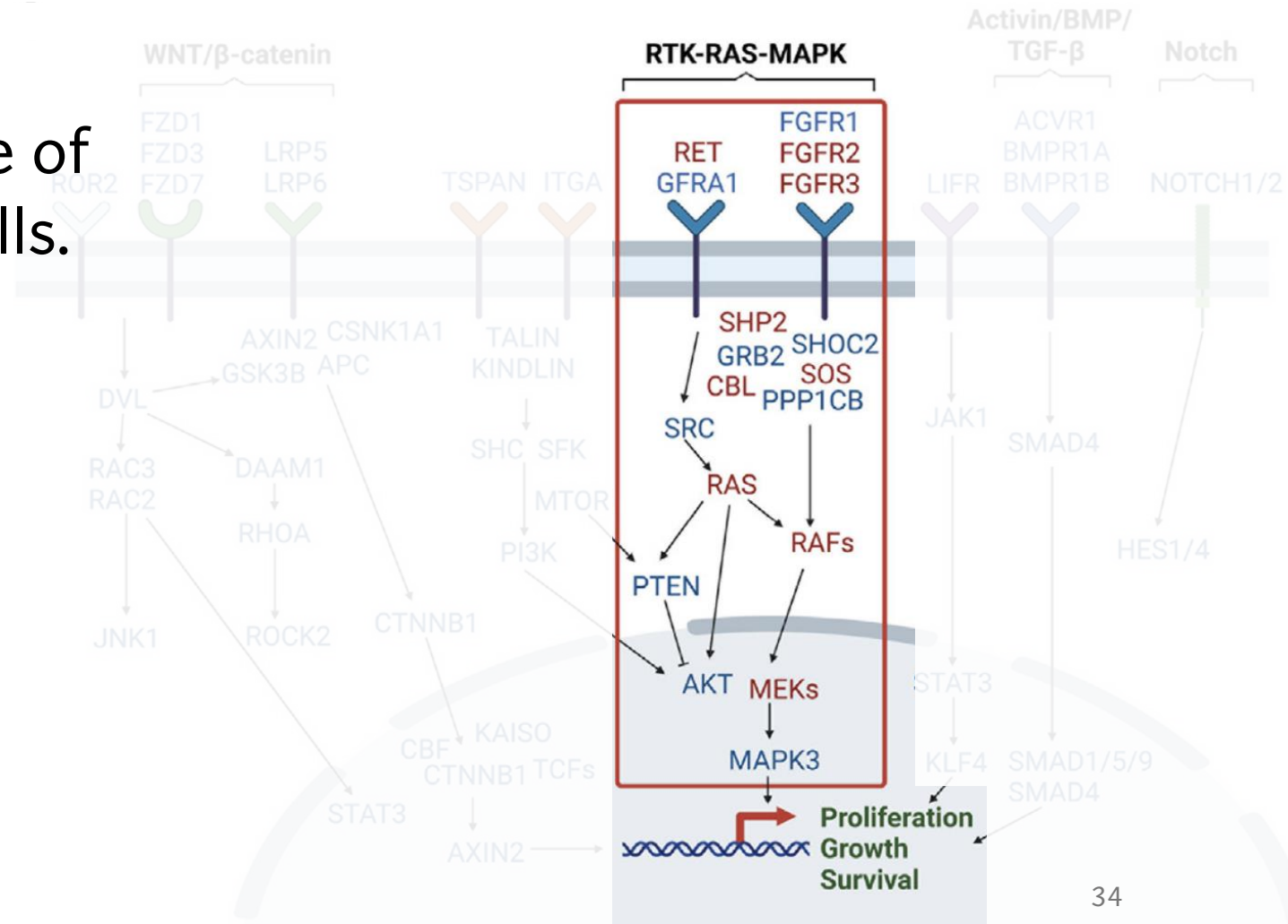
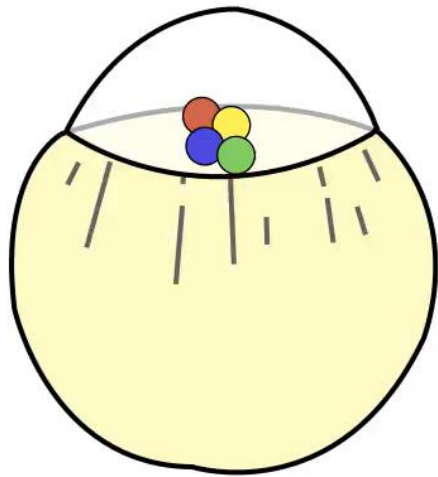
Null hypothesis: $s = 0$.

The likelihood is maximized at $s = -0.19$.

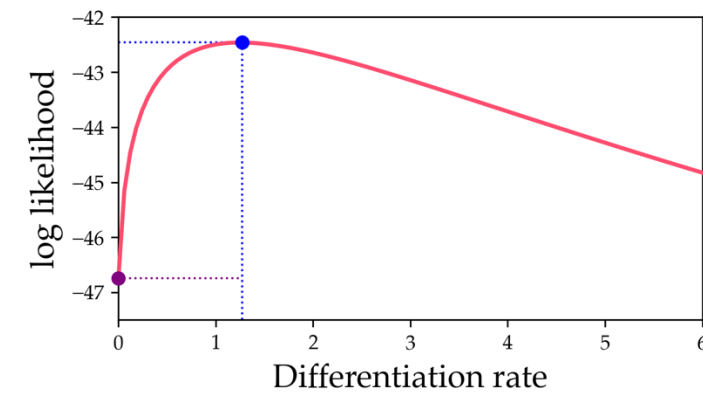
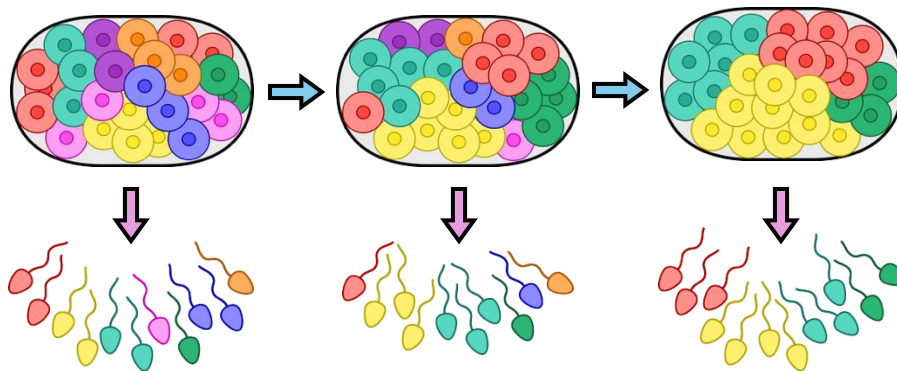
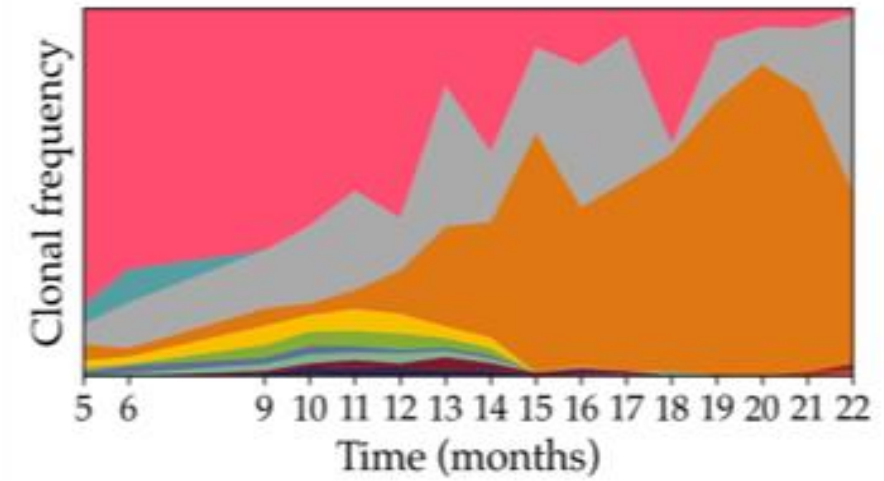
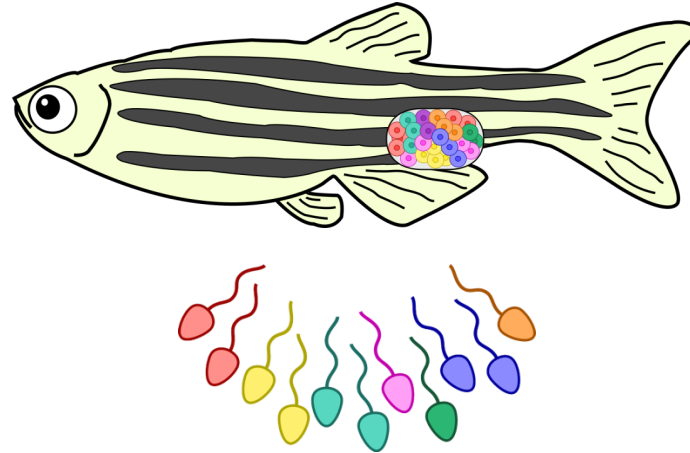
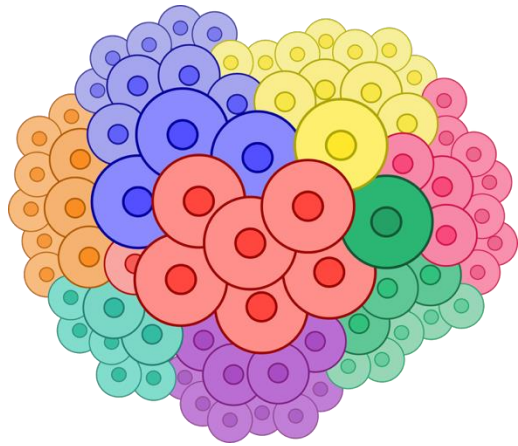
The test statistic λ is 8.36.

Introducing selection experimentally

Insert a mutation in one of the primordial germ cells.



Summary



Acknowledgements



Fred Adler
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Jamie Gagnon
(lab PI)



Jenna Weber



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Let's collaborate!
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Thank you!

